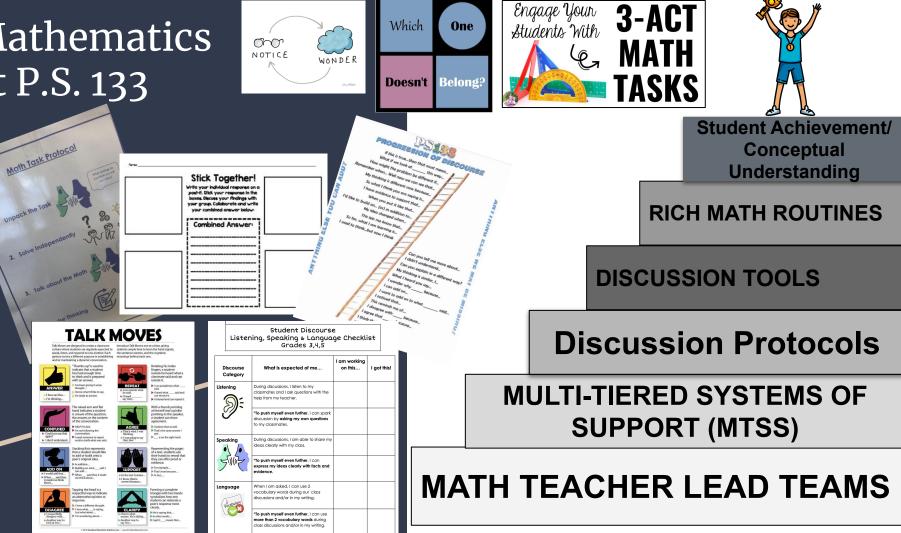
# **Illustrative Mathematics** LEARN MATH FOR LIFE

# **Illustrative Mathematics at P.S. 133**

# June 5th, 2023 8:30am - 10:30am

Math Leads: Nicolaou, Scarpulla, Reilly, Rosica, Barilla, Gold

# Mathematics at P.S. 133



# Routines

Math routines are embedded in each lesson and directly connect with the standards addressed in the lesson.

| Warm-up Routines          | Lesson Activity Routines             |
|---------------------------|--------------------------------------|
| Act It Out                | Math Language Routines (MLRs)        |
| Choral Count              | MLR1: Stronger and Clearer Each Time |
| Estimation Exploration    | MLR2: Collect and Display            |
| How Many Do You See?      | MLR3: Clarify, Critique, Correct     |
| Notice and Wonder         | MLR4: Information Gap                |
| Number Talk               | MLR5: Co-craft Questions             |
| Questions About Us        | MLR6: Three Reads                    |
| True or False?            | MLR7: Compare and Connect            |
| What Do You Know About?   | MLR8: Discussion Supports            |
| Which One Doesn't Belong? | Other Lesson Activity Routines       |

### 3. Establish a Mathematics Instructional Focus

Each district will select a mathematics focus from the below list for the 2022-2023 school year to support their schools in implementing instruction aligned to the vision.

- A. Provide mathematics instruction that is culturally responsive and sustaining by:
  - promoting pedagogical knowledge and mathematical thinking,
  - leveraging cultural and linguistic funds of knowledge, and
  - attending to issues of power and social justice in mathematics education.
- B. Implement high-quality, coherent, research-based core mathematics curriculum. Ensuring that every child has access to a coherent trajectory of learning, aligned to the Next Generation Learning Standards, that provides opportunities for individual and collaborative sense-making, through open tasks that connect students' understanding of the real world to mathematical concepts.
- Integrate mathematics instructional routines into instruction. Instructional Routines support all students, but are essential for supporting students in need of intervention, students with disabilities, as well as multilingual learners to participate in academic discourse and mathematics sense-making.
  - D. Focus on NYC Public Schools' Foundational Mathematics Standards by grade level.

These standards support teachers in knowing where to invest additional time so that students can develop a strong foundation, including solid conceptual understanding, procedural fluency, and the ability to apply math to solve problems inside and outside the math classroom.

| Which one | e doesn't belong? |   |  |
|-----------|-------------------|---|--|
| A         |                   | В |  |
|           |                   |   |  |
| c         |                   | D |  |

| What is th | e value | of 0.42 | ÷ 52 |
|------------|---------|---------|------|
| wind is th | e value | 01 0.42 | · ): |

Record an estimate that is:

- How do you know 0.42 ÷ 5 is more than 8 hundredths? ٠
- Why is 8 hundredths a good estimate for the value of 0.42 ÷ 5?

**Vertically Aligned Centers** 

IM K-5 МАТН 🕁

### **Centers Navigation Tool**

Click on your grade level to explore your grade's centers:

| Counting, P<br>Fractions (wit |   |   |  |  |  | )  | Operations & A<br>and Fractions  |  |   |  |   |  |   | Measurement,   | Dat   | a a   | nd (  | Seo   | me  |
|-------------------------------|---|---|--|--|--|--|--|--|---|--|---|--|---|--|---|---|---|---|---|
|                               | к   | 1   | 2  | 3  | 4  | 5  |  | к  | 1   | 2  | 3   | 4  | 5   |  | к   | 1   | 2   | 3   | 4   |
| Tower Build                   | V   |   |  |  |  |  | Roll and Add   | ~  |   |  |   |  |   | Connecting Cubes   | ~   | -   |   |   |   |
| ss, Same, More                | ~   |   |  |  |  |  | Find the Value of Expressions  | ~  |   |  |   |  |   | Build Shapes   | ~   |   |   |   |   |
| traction Towers               | V   |   |  |  |  |  | Make or Break Apart Numbers  | ~  |   |  |   |  |   | Pattern Blocks   | ~   |   |   |   |   |
| Grab and Count                | V   | ~   |  |  |  |  | 5 Frames   | ~  |   |  |   |  |   | Match Mine   | ~   | ~   |   |   |   |
| Number Races                  | V   | ~   |  |  |  |  | Math Fingers   | ~  |   |  |   |  |   | Geoblocks  | ~   | ~   |   |   |   |
| ting Collections              | ~   | ~   |  |  | -  |  | Bingo  | ~  |   |  |   |  |   | Which One?   | ~   | ~   | ~   | ~   | ~   |
| Write Numbers                 |   | ~   | ~  |  |  |  | Math Libs  | ~  |   |  |   |  |   | Picture Books  | ~   | ~   | ~   | ~   | v   |
| mbers in Order                |   | ~   | ~  |  | ~  | ~  | Find the Pair  | ~  | V   |  |   |  |   | Sort and Display   |   | ~   | ~   | ~   |   |
| test of them All              |   | ~   | ~  |  | ~  | ~  | Check it Off   | ~  | ~   |  |   |  |   | Estimate and Meausure  |   | ~   | ~   | ~   | v   |
| nber Line Scoot               |   |   | ~  | V  |  |  | What's Behind my Back?   | ~  | ~   | ~  |   |  |   | Target Measurements  |   | ~   | ~   | ~   | v   |
| lystery Number                |   | ~   | ~  | V  | V  | ~  | Shake and Spill  | ~  | ~   | V  |   |  |   | How are They the Same?   |   | ~   | ~   | ~   | v   |
| Secret Fractions              |   |   |  | V  | V  |  | Math Stories   | ~  | ~   | ~  |   |  |   | Can You Draw it?   |   | ~   | ~   | ~   | v   |
| Tic Tac Round                 |   |   |  | V  | V  | V  | Capture Squares  |  | ~   | V  | V   | ~  |   | Would You Rather?  |   |   | ~   |   | v   |
|                               |   |   |  |  |  |  | Target Numbers   |  | ~   | V  | ~   |  | ~   | Creating Line Plots  |   |   | ~   | ~   | v   |
|                               |   |   |  |  |  |  | How Close?   |  | ~   | V  | ~   | ~  | ~   | Can You Build It?  |   |   |   | ~   | v   |
|                               |   |   |  |  |  |  | Compare  |  | ~   |  | ~   | ~  | ~   | Symmetrical Designs  |   |   |   |   | v   |
|                               |   |   |  |  |  | Five i   | in a Row: Addition and Subtraction   |  | ~   | V  | ~   |  | ~   |  |   |   |   |   |   |
|                               |   |   |  |  | Fi   | ve in  | a Row: Multiplication and Division   |  |   |  | ~   | ~  | ~   |  |   |   |   |   |   |
|                               |   |   |  |  | Nu   | mber   | Puzzles: Addition and Subtraction  |  | V   | V  | ~   | ~  | ~   |  |   |   |   |   |   |
|                               |   |   |  |  | Nur  | nber   | Puzzles:Multiplication and Division  |  |   |  |   | V  | ~   |  |   |   |   |   |   |
|                               |   |   |  |  |  |  | Jump the Line  |  |   | ~  |   | ~  | ~   |  |   |   |   |   |   |
|                               |   |   |  |  |  |  | Rectangle Rumble   |  |   |  | ~   | ~  | ~   |  |   |   |   |   |   |
|                               |   |   |  |  |  |  | Rolling for Fractions  |  |   |  | V   | ~  | V   |  |   |   |   |   |   |
|                               |   |   |  |  |  |  | Find the Number  |  |   |  |   |  |   |  |   |   |   |   |   |
|                               | Tower Build<br>Ss, Same, More<br>raction Towers<br>irab and Count<br>Number Races<br>Write Numbers<br>mbers in Order<br>test of them All<br>aber Line Scoot<br>extery Fractions | Fractions (without<br>ss, Same, More<br>ss, Same, More<br>araction Towers<br>frab and Count<br>Number Races<br>Write Numbers<br>ing Collections<br>Write Numbers<br>test of them All<br>bers In Order<br>tests of them All<br>ther Line Scoot<br>ystery Number<br>erret Fractions | Fractions (without O<br>Tower Build<br>Ss, Same, More<br>Sraband Count<br>Traction 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Watch Your Remainder

V V

### 2. Develop a Multi-Tiered System of Supports for Mathematics (MTSS-M)

By the end of the 2023-2024 school year, every school will develop a fully implemented MTSS for Mathematics. The expectations for the 2022-2023 are:

- Administer math screeners three times a year.
- Utilize data from multiple sources to identify, implement and progress monitor improvements to core instruction.
- Provide interventions focused on NYC Public Schools Foundational Mathematics Standards if students fall behind, even after strengthening core instruction.

| Five in a Row Ad | ddition and Subtracti | on Stage 3 Gamebo | ard | 5 in a<br>ROW |
|------------------|-----------------------|-------------------|-----|---------------|
| 12               | 14                    | 12                | 8   | 11            |
| 15               | 17                    | 16                | 10  | 19            |
| 18               | 13                    | FREE              | 15  | 14            |
| 9                | 17                    | 10                | 13  | 7             |
| 19               | 16                    | 11                | 9   | 18            |

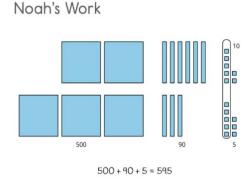
| sum of the 2 n<br>Partner B: Mov<br>sum with a cou | a paper clip on 2 i<br>umbers with a co<br>e 1 of the paper o<br>inter.<br>e first partner to o | unter.<br>:lips, add the nun | nbers, and cover t |     |
|--|---|------------------------------|--------------------|-----|
| 704  | 669   | 621                          | 442                | 784 |
| 497  | 695   | 323                          | 956                | 44  |
| 586  | 413   | 784                          | 576                | 614 |
| 297  | 386   | 378                          | 867                | 532 |
| 873  | 99  | 134                          | 531                | 665 |
| 263  | 100   | 352                          | 65                 | 10  |
| 34   | 432   | 604                          | 313                | 521 |

Five in a Row Addition and Subtraction Stage 7 Gameboard

# Open Tasks that Promote Discussion

2nd Grade Task

Noah and Kiran showed how they found the value of 267+338.



100 + 300 = 500 60 + 30 = 90 7 + 8 = 15 500 + 90 + 15 500 + 90 + 10 + 5500 + 100 + 5 = 605

Kiran's work

- B. Implement high-quality, coherent, research-based core mathematics curriculum. Ensuring that every child has access to a coherent trajectory of learning, aligned to the Next Generation Learning Standards, that provides opportunities for individual and collaborative sense-making, through open tasks that connect students' understanding of the real world to mathematical concepts.
  - <sup>1)</sup> How is Noah and Kiran's work the same? How is it different?
  - <sup>2)</sup> Which student found the correct value? Explain or show your thinking.



# Open Tasks that Promote Discussion

4th Grade Task

### **Questionable Lockers**

In your small group, discuss what you notice and wonder about the picture.



The picture shows lockers in a school hallway.

The 20 students in Tyler's fourth-grade class are playing a game in a hallway that is lined with 20 lockers in a row.

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20

Implement high-quality, coherent, research-based core mathematics curriculum.

mathematical concepts.

Ensuring that every child has access to a coherent trajectory of learning, aligned to the Next

Generation Learning Standards, that provides opportunities for individual and collaborative

sense-making, through open tasks that connect students' understanding of the real world to

- The first student starts with the first locker and goes down the hallway and opens all the lockers.
- The second student starts with the second locker and goes down the hallway and shuts every other locker.
- The third student stops at every third locker and opens the locker if it is closed or closes the locker if it is open.

This process continues until all 20 students in the class have touched the lockers.



Launch

Unit 1 • Lesson 6 • Activity 1

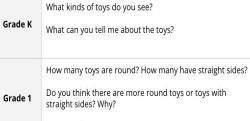
# **Embracing Authentic Discussions**

# Talking Math



### Focus on Data

Note: Invitational prompts are sometimes tagged to prior grade level standards.



(K.MD and 1.MD)

Complete the sentences:

There are 2 more \_\_\_\_\_ than \_\_\_\_\_. There are 8

Grade 2 In this picture there are groups of\_ The number of is less than the number of (1.MD and 2.MD.10)

Pick four kinds of toys and count them.

If you made a picture graph about the number of each Grade 3 kind, what could you use as a symbol for each toy?

(2.MD)

# Invitational 1 **Talking Math**

## Invitational 2

| AND   | Grade K | What can you count in the picture? How would you count them? (K.CC)  |
|---|---------|--|
|   | Grade 1 | How many more puppies would make 10 puppies?<br>How many puppies could join these puppies so there<br>would be <b>more</b> than 10 puppies in all? Explain.<br>(K.OA.4 and 1.OA.2)                 |
|   | Grade 2 | Some of these puppies jumped out of the basket and<br>2 were left in the basket. How many puppies jumped<br>out? Write an equation to show the situation. (1.OA.1)                                 |
| Focus on Counting & Operations  | Grade 3 | There are 5 puppies in the basket. Count by fives to<br>30. How could counting by fives help you find out how<br>many puppies would be in 6 such baskets?<br>(2.NBT.2 and 3.OA.1)                  |
| Note: Invitational prompts are<br>sometimes tagged to prior grade level<br>standards. | Grade 4 | We see 5 puppies can sit in a basket. How many<br>baskets would there need to be for 45 puppies?<br>How many baskets would be needed for 52 puppies?<br>Explain your thinking. (3.OA.3 and 4.OA.3) |
|   | Grade 5 | Two of these puppies weigh 263 grams each and three of the puppies weigh 315 grams each. Find the weight of all the puppies. (4.NBT.4 and 5.OA.1)  |

### **ENGAGING STUDENTS: SPARKING CURIOSITY**

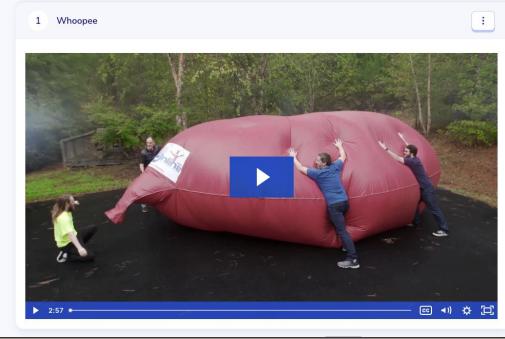
### 5.8 Inspire Math Video: First Showing

♥ Actions ♥

Instructional video Ma

ш

o Materials About this video



### **Teaching notes**

Assign 🗸

### Materials:

- Video: Whoopee!
- Chart paper with a chart with three column headings: record-setting things, what we might count or measure, measurement units

### Instruction:

- "We will watch a short video together. Be prepared to share your thinking and answer some questions."
- Show the video Whoopee!.
- "What are some record-setting events we saw in the video?" (highest climber, fastest runner, largest pumpkin, farthest trip)
- Record responses in the column labeled "record-setting events".
- Note: Students will have another opportunity to add to this list after watching the video a second time. The goal here is not to capture all the things, just to start a list and revisit measurement units. Here is a sample completed table.
- "What do you think is measured for each world-record? What else could be measured? To be measured will be

### Standards for Mathematical Practice

- Make sense of problems and persevere in solving them.
- Reason abstractly and quantitatively.
- Construct viable arguments and critique the reasoning of others.
- Model with mathematics.
- Use appropriate tools strategically.
- Attend to precision.
- Look for and make use of structure.
- Look for and express regularity in repeated reasoning.

| Standard for Mathematical<br>Practice                                     | Student Friendly<br>Language   |
|---|--|
| 1. Make sense of problems and persevere in solving them.                  | <ul> <li>I can try many times to<br/>understand and solve a<br/>math problem.</li> </ul>               |
| 2. Reason abstractly<br>and quantitatively.                               | I can think about the math problem in my head, first.  |
| 3. Construct viable arguments<br>and critique the reasoning<br>of others. | I can make a plan, called a strategy, to solve the problem and discuss other students' strategies too. |
| 4. Model with mathematics.  | I can use math symbols and<br>numbers to solve the<br>problem.   |
| 5. Use appropriate tools strategically.                                   | I can use math tools,<br>pictures, drawings, and<br>objects to solve the problem                       |
| 6. Attend to precision.   | I can check to see if my<br>strategy and calculations<br>are correct.                                  |
| 7. Look for and make use of structure                                     | I can use what I already<br>know about math to solve<br>the problem.                                   |
| 8. Look for and express regularity in repeated reasoning.                 | I can use a strategy that I<br>used to solve another math<br>problem.                                  |

# Welcome to Imagine Learning Classroom for New York City!

Wiki Included in

2



### Welcome to Imagine Learning EL Education K-8 Language Arts Curriculum

The EL Education K-8 Language Arts Curriculum was created to support your students to build skills and content knowledge, to meet college- and career-ready standards, and, at the same time, to become more confident and collaborat...

# 

### Illustrative Mathematics® K-12 with Accelerated 6/7

ILLUSTRATIVE MATHEMATICS



### EL EDUCATION LANGUAGE ARTS

# **Materials/Teacher Prep**

Certain parts of the lesson (card sorts, some activities) are not in the student workbook

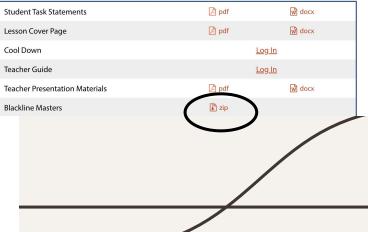
| Grade 2 🗸 🗸 | Unit 1 🗸 | Lesson                                       |  |  |  |  |  |  |  |  |  |  |
|-------------|----------|--|--|--|--|--|--|--|--|--|--|--|
| Glade 2     | onici    | 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 |  |  |  |  |  |  |  |  |  |  |

### LESSON 1

### Add and Subtract Within 10

| PREPARATION                 | LESSON   | Print Formatted<br>Materials | T |
|-----------------------------|--|------------------------------|---|
|                             |  |                              | 2 |
| Lesson Purpose              | The purpose of this lesson is for students to add and subtract within 10.  |                              | l |
| <b>Required Materials</b>   | Materials to Gather  |                              | ( |
|                             | Connecting cubes or counters   |                              | 1 |
|                             |  |                              | 1 |
|                             | Materials to Copy  |                              | E |
|                             | Number Cards (0-10)  |                              |   |
| <b>Required Preparation</b> | Activity 1:  |                              |   |
|                             | <ul> <li>Create a set of number cards for each group of 2.</li> <li>The number cards will be used in upcoming lessons and thoughout the year. Consid cards on cardstock or laminating them for future use.</li> <li>Create the math community poster for display in the lesson synthesis.</li> </ul> | er copying the               |   |

Teachers with a valid work email address can <u>click here to register or sign in</u> for free access to Cool Down, Teacher Guide, and PowerPoint materials.



# Support for

# Families

# View materials for: GRADE K GRADE 1 GRADE 2 GRADE 2 En Español: Kínder En Español: Grado 1 En Español: Grado 2 GRADE 3 GRADE 4 GRADE 5 GRAD

### **For Teachers**

**For Families** 

View materials for:

